

Unit 6: Radicals Review

Simplify. Use absolute value signs when necessary.

$$1) \frac{\sqrt[5]{-224m^5n^3}}{-2m\sqrt[5]{7n^3}}$$

$$2) \frac{\sqrt{192x^3y}}{8|x|\sqrt{3xy}}$$

$$3) \frac{\sqrt{216x^3y^4}}{6y^2|x|\sqrt{6x}}$$

$$4) \frac{\sqrt{20xy^2}}{2|y|\sqrt{5x}}$$

$$5) \frac{\sqrt{150u^4v^2}}{5u^2|v|\sqrt{6}}$$

$$6) \frac{\sqrt[3]{162x^5y^5}}{3xy\sqrt[3]{6x^2y^2}}$$

$$7) \frac{\sqrt[3]{20p^3} \cdot \sqrt[3]{25p^3}}{5p^2\sqrt[3]{4}}$$

$$8) \frac{\sqrt{5x^2} \cdot \sqrt{3x^2}}{x^2\sqrt{15}}$$

$$9) \frac{-5\sqrt[4]{3m} \cdot \sqrt[4]{2m^3}}{-5|m|\sqrt[4]{6}}$$

$$10) \frac{-3\sqrt[6]{128x^7} \cdot \sqrt[6]{192x^5}}{-12x^2\sqrt[6]{6}}$$

$$11) \frac{3\sqrt{5x} \cdot -5\sqrt{10x^3}}{-75x^2\sqrt{2}}$$

$$12) \frac{-4\sqrt[3]{-4a^2} \cdot -4\sqrt[3]{16a^4}}{-64a^2}$$

$$13) \frac{\sqrt{3v^4}}{\sqrt{2v^2}}$$

$$\frac{\sqrt{3}v^2}{\sqrt{2}v}$$

$$\frac{v\sqrt{6}}{2}$$

$$14) \frac{\sqrt{5r}}{\sqrt{2r}}$$

$$\frac{\sqrt{10}}{2}$$

$$15) \frac{5}{5\sqrt{2x^2y^4}}$$

$$\frac{\sqrt{2}}{2y^2|x|}$$

$$16) \frac{5\sqrt{5x^3}}{\sqrt{3x^4}}$$

$$\frac{5\sqrt{15x}}{3|x|}$$

$$17) \frac{4\sqrt{3r^4}}{\sqrt{5r^2}}$$

$$\frac{4|r|\sqrt{15}}{5}$$

$$18) \frac{\sqrt{20x^4y^2}}{2\sqrt{12x^2y^3}}$$

$$\frac{|x|\sqrt{15y}}{6|y|}$$

$$19) \frac{-2\sqrt{45} - 3\sqrt{12} + 2\sqrt{27}}{-6\sqrt{5}}$$

$$20) \frac{-\sqrt{27} - \sqrt{27} + 2\sqrt{2}}{-6\sqrt{3} + 2\sqrt{2}}$$

$$21) \frac{3\sqrt{3} - \sqrt{6} - 2\sqrt{3}}{\sqrt{3} - \sqrt{6}}$$

$$22) \frac{-\sqrt{27} + 3\sqrt{27} - \sqrt{24}}{6\sqrt{3} - 2\sqrt{6}}$$

$$23) \frac{-2\sqrt[3]{40} - \sqrt[3]{162} + 3\sqrt[3]{5}}{-\sqrt[3]{5} - 3\sqrt[3]{6}}$$

$$24) \frac{3\sqrt{8} + 2\sqrt{8} - \sqrt{45}}{10\sqrt{2} - 3\sqrt{5}}$$

Simplify.

$$25) \frac{(-1 + 5\sqrt{2})(-2 + \sqrt{2})}{12 - 11\sqrt{2}}$$

$$26) \frac{(2 + \sqrt{2})(-3 + \sqrt{2})}{-4 - \sqrt{2}}$$

$$27) \frac{(\sqrt{5} - 2)(-\sqrt{5} - 2)}{-1}$$

$$28) \frac{(\sqrt{2} - 4\sqrt{5})(\sqrt{5} + \sqrt{5})}{2\sqrt{10} - 40}$$

$$29) (1 - 3\sqrt{5})(3 - 3\sqrt{5})$$

$$48 - 12\sqrt{5}$$

$$30) (-\sqrt{5} + \sqrt{3})(\sqrt{5} + \sqrt{3})$$

$$-2$$

Simplify. Assume that all variables are positive.

$$31) \frac{4n}{8\sqrt{6n^2}}$$

$$\frac{\sqrt{6}}{12}$$

$$32) \frac{4\sqrt{7x^2}}{\sqrt{5x^4}}$$

$$\frac{4\sqrt{35}}{5x}$$

$$33) \frac{\sqrt{4n^3}}{\sqrt{5n^2}}$$

$$\frac{2\sqrt{5n}}{5}$$

$$34) \frac{\sqrt{2b^3}}{4\sqrt{7b^2}}$$

$$\frac{\sqrt{14b}}{28}$$

$$35) \frac{5}{\sqrt[3]{25a^2}}$$

$$\frac{\sqrt[3]{5a}}{a}$$

$$36) \frac{2n}{\sqrt[4]{n^2}}$$

$$2\sqrt[4]{n^2}$$

$$37) \frac{x^2}{\sqrt[3]{2x^2}}$$

$$\frac{x\sqrt[3]{4x}}{2}$$

$$38) \frac{2}{\sqrt[3]{n}}$$

$$\frac{2\sqrt[3]{n^2}}{n}$$

$$39) \frac{4\sqrt{10} - \sqrt{5}}{-3 + 4\sqrt{7}}$$

$$\frac{12\sqrt{10} + 16\sqrt{70} - 3\sqrt{5} - 4\sqrt{35}}{103}$$

$$40) \frac{8 + \sqrt{5}}{\sqrt{3} - 4}$$

$$\frac{-8\sqrt{3} - 32 - \sqrt{15} - 4\sqrt{5}}{13}$$

$$41) \frac{7 + \sqrt{2}}{2\sqrt{2} + 5\sqrt{5}}$$

$$\frac{-14\sqrt{2} + 35\sqrt{5} - 4 + 5\sqrt{10}}{117}$$

$$42) \frac{-6 - 7\sqrt{7}}{\sqrt{6} - 7\sqrt{10}}$$

$$\frac{6\sqrt{6} + 42\sqrt{10} + 7\sqrt{42} + 49\sqrt{70}}{484}$$

Solve each equation. Remember to check for extraneous solutions.

$$43) \sqrt{18 - 2x} = \sqrt{2x - 2}$$

$$\{5\}$$

$$44) 11 = 10 + \sqrt{8 - x}$$

$$\{7\}$$

$$45) \sqrt{v - 6} = \sqrt{2v - 20}$$

$$\{14\}$$

$$46) 1 + \sqrt{-1 - 37b} = 7$$

$$\{-1\}$$

$$47) \sqrt{\frac{b}{2}} - 6 = -5$$

$$\{2\}$$

$$48) \sqrt{6 - v} = v$$

$$\{2\}$$

Simplify.

$$49) 8^{\frac{2}{3}} \cdot 4^{\frac{1}{5}}$$

$$2^{\frac{12}{5}}$$

$$50) 6^{\frac{1}{4}} \cdot 36^{\frac{2}{5}}$$

$$6^{\frac{21}{20}}$$

$$51) 125^{\frac{2}{3}} \cdot 25^3$$

$$5^8$$

$$52) 4^{\frac{5}{4}} \cdot 32^{\frac{1}{3}}$$

$$2^{\frac{11}{3}}$$

$$53) 3^{\frac{2}{7}} \cdot 81^{\frac{2}{5}}$$

$$3^{\frac{66}{35}}$$

$$54) 7^{\frac{8}{3}} \cdot 49^{\frac{3}{4}}$$

$$7^{\frac{25}{6}}$$