

7.2 Solving Systems by Graphing

The solution to a system of equations is where the graphs intersect.

Let's refresh our memory on how to graph each kind of equation:

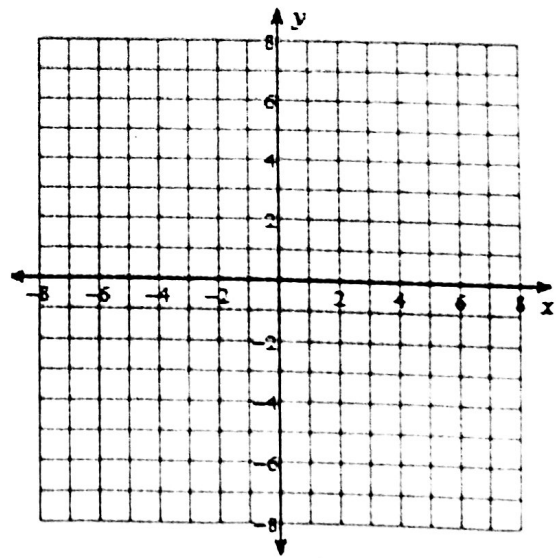
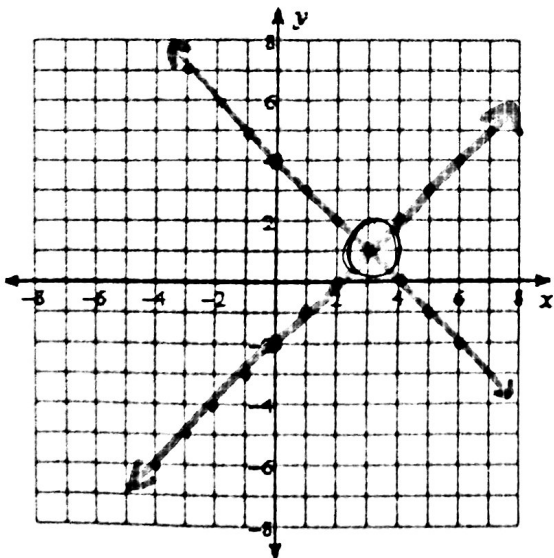
| Linear | Quadratic | Circle |
|--|---|---|
| $y = mx + b$ ↑ slope ↑ y-intercept | 1) $y = ax^2 + bx + c$ 2) $y = a(x-h)^2 + k$ 3) $y = a(x-p)(x-q)$ | $(x-h)^2 + (y-k)^2 = r^2$ (h,k) is the center r is the radius |
| | Find the vertex*, then use 1a 3a 5a *can use calculator | |

1) Solve each system by graphing.

a) $y = x - 2$
 $y = -x + 4$

$(3, 1)$

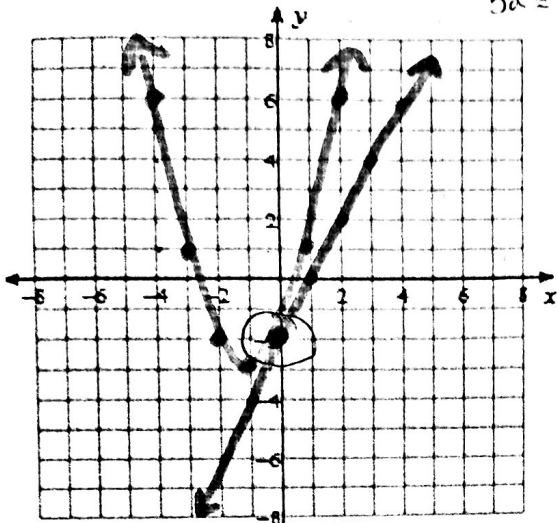
b) $y = -2x + 4$
 $y = -\frac{1}{2}x - 2$



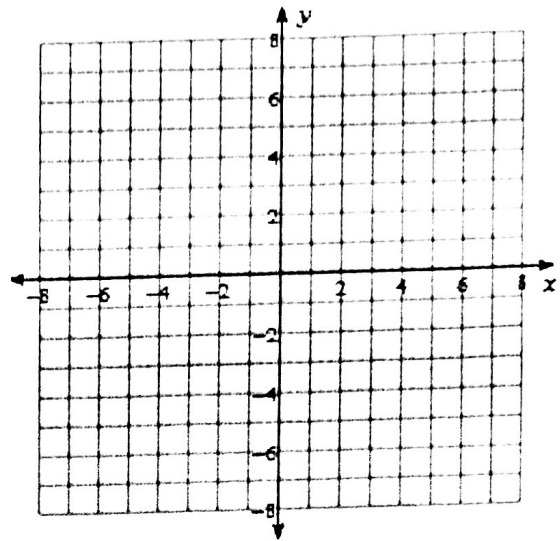
c) $y = x^2 + 2x - 2$ $V: (-1, -3)$
 $y = 2x - 2$

$a = 1$
 $1a = 1(1) = 1$
 $3a = 3(1) = 3$
 $5a = 5(1) = 5$

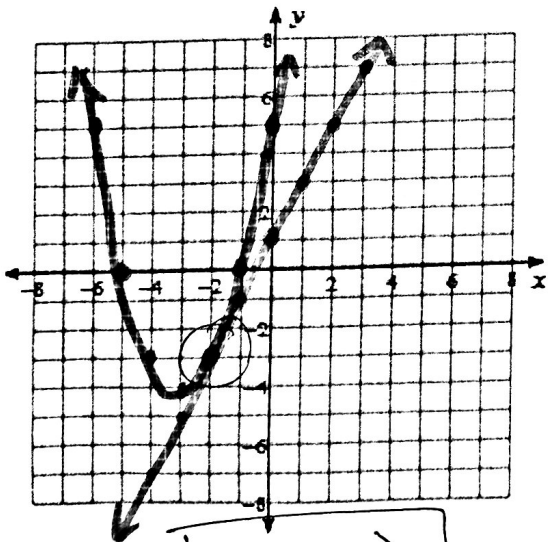
d) $y = 3x$
 $y = x^2 + 4x - 2$



$(0, -2)$

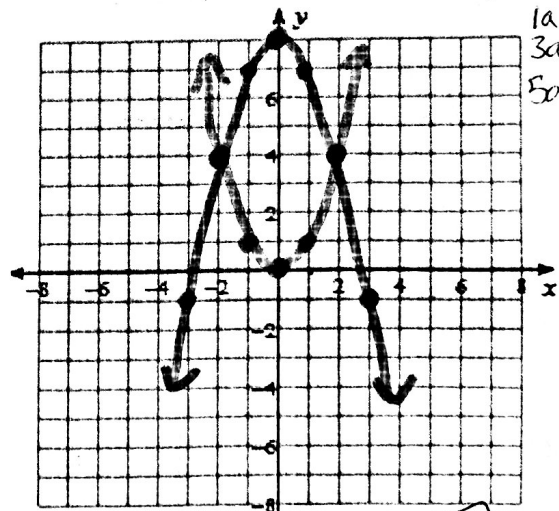


e) $y = 2x + 1$
 $y = (x + 5)(x + 1)$



$(-2, -3)$

f) $y = x^2 = (x - 0)^2 + 0$ $V: (0, 0)$ $a = 1$
 $y = -x^2 + 8$ $3a = 3$
 $= -(x - 0)^2 + 8$ $V: (0, 8)$ $5a = 5$
 $a = -1$

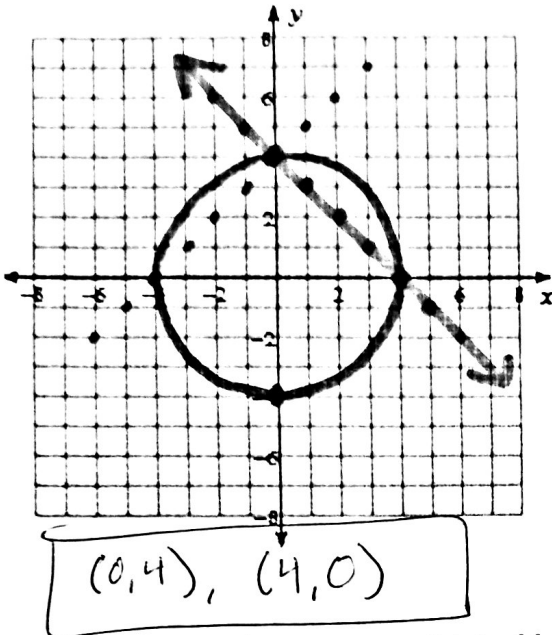


$1a = -1$
 $3a = -3$
 $5a = -5$

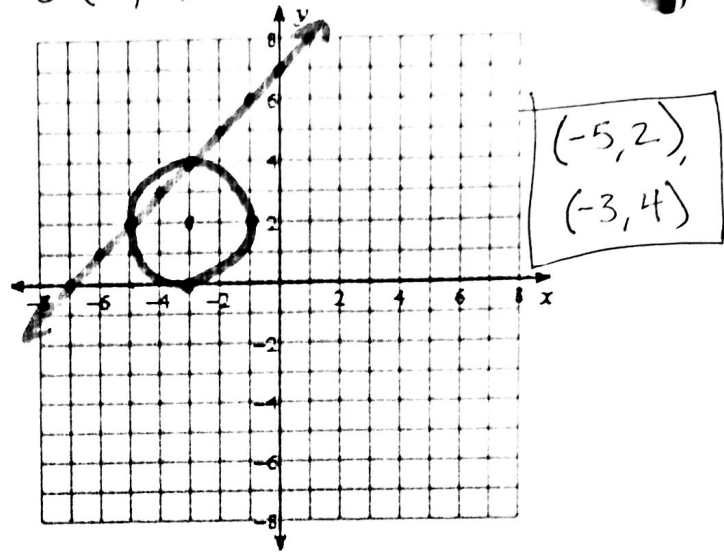
$(-2, 4), (2, 4)$

If the graphs do not intersect, then there is no solution.

$y = -x + 4$
 g) $y = 4 - x$
 $x^2 + y^2 = 16$

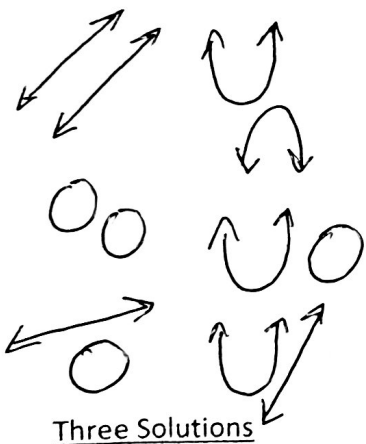


h) $y = x + 7$
 $(x + 3)^2 + (y - 2)^2 = 4$ ← $\sqrt{r^2} = \sqrt{4}$
 $r = 2$
 $C: (-3, 2) \quad r = 2$

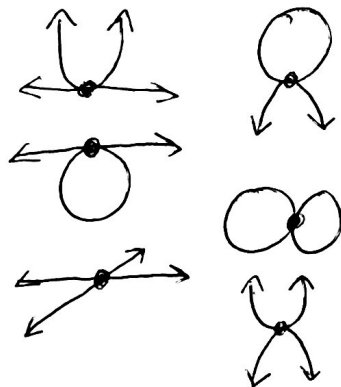


2) Draw as many examples as you can think of for each category.

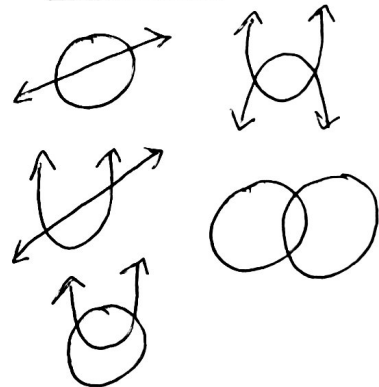
No Solution



One Solution



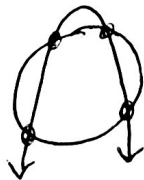
Two Solutions



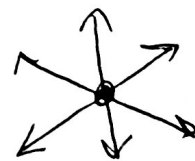
Three Solutions



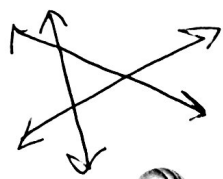
Four Solutions



System of 3+ equations



One solution



No solution

* Solutions are where all equations intersect