

5.5 Graphing from Intercept Form

What information do you need in order to graph a quadratic function?

Vertex & a-value

* The x-intercepts represent the solutions to the equation

INTERCEPT FORM:

$$y = a(x-p)(x-q)$$

Opposite

p & q represent the x-intercepts

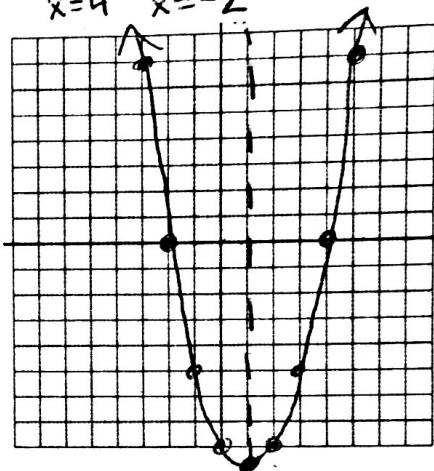
Let's practice graphing a parabola from intercept form:

How to find the Vertex in Intercept Form:

- 1) Find & plot x-intercepts
- 2) Find axis of symmetry by going halfway between x-intercepts
- 3) Plug in axis of symmetry into equation to get y of vertex
 ex: $x=1$ $y = (1-4)(1+2)$
 $= -9$
 Vertex: $(1, -9)$

Graph $y = (x-4)(x+2)$

$$x=4 \quad x=-2$$



$$a=1$$

$$1a=1$$

$$3a=3$$

$$5a=5$$

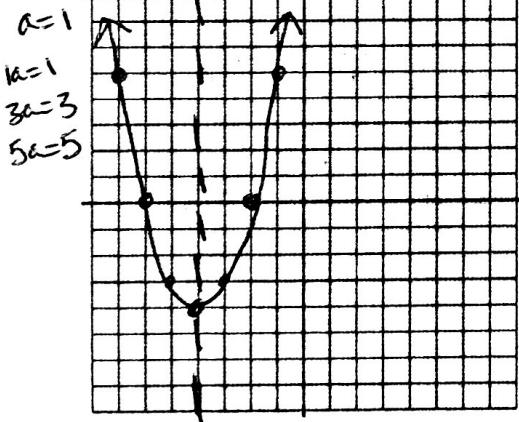
$$7a=7$$

Example 1: Graph the following quadratic equations

a) $y = (x+2)(x+6)$

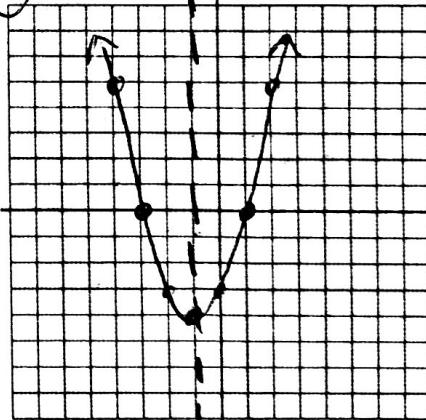
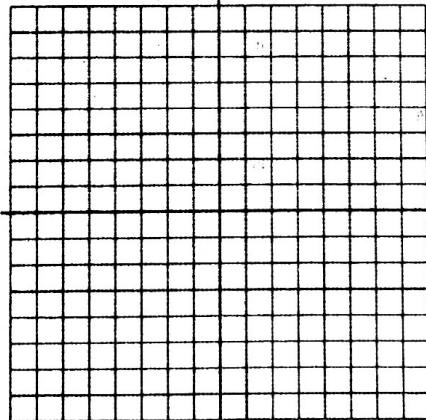
b) $y = x(x-8)$

c) $y = (x-1)(x+3)$



$$\begin{aligned} x &= -4 & y &= (-4+2)(-4+6) \\ & & &= (-2)(2) \\ & & &= -4 \end{aligned}$$

Vertex $(-4, -4)$



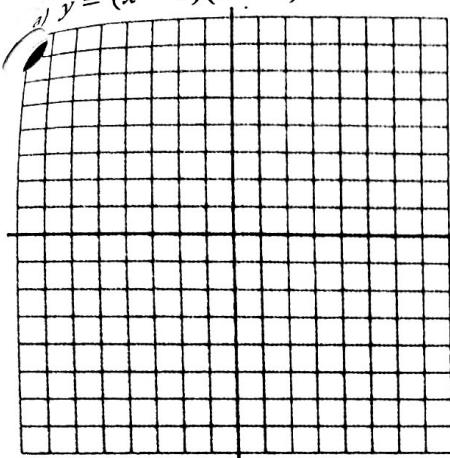
$$\begin{aligned} x &= -1 & y &= (-1-1)(-1+3) \\ & & &= (-2)(2) \\ & & &= -4 \end{aligned}$$

Vertex $(-1, -4)$

$$\begin{aligned} a &= 1 \\ 1a &= 1 \\ 3a &= 3 \\ 5a &= 5 \end{aligned}$$

Example 2: Graph the following quadratic equations

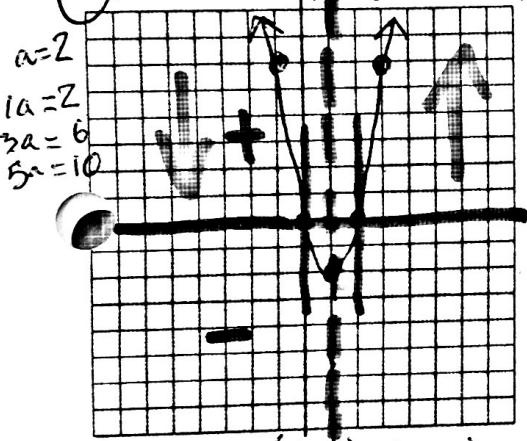
a) $y = (x - 5)(x - 1)$



x-intercept(s):

Vertex: $y = 2(1)(1-2) = -2$

d) $y = 2x(x - 2) = 2(x+0)(x-2)$



x-intercept(s): $(0, 0), (2, 0)$

y-intercept: $(0, 0)$

Axis of Symmetry: $x = 1$

Vertex: $(1, -2)$

Max/min value: -2

Domain: $(-\infty, \infty)$

Range: $[-2, \infty)$

Increasing: $(1, \infty)$

Decreasing: $(-\infty, 1)$

Positive: $(-\infty, 0) \cup (2, \infty)$

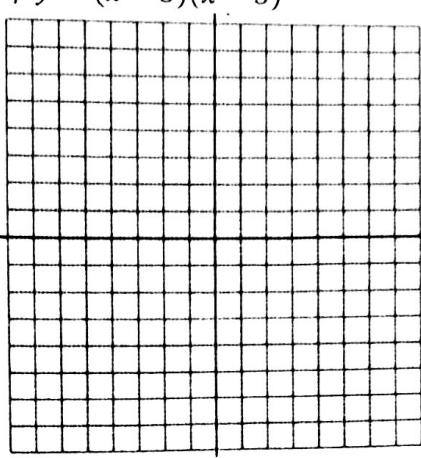
Negative: $(0, 2)$

End behavior:

As $x \rightarrow \infty, y \rightarrow \infty$

As $x \rightarrow -\infty, y \rightarrow \infty$

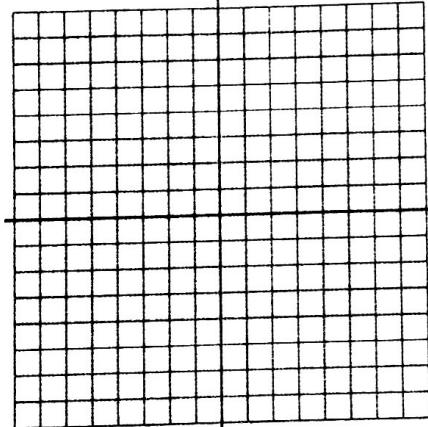
b) $y = (x - 3)(x - 5)$



x-intercept(s):

Vertex:

e) $y = (x + 2)(x - 2)$



x-intercept(s):

y-intercept:

Axis of Symmetry:

Vertex:

Max/min value:

Domain:

Range:

Increasing:

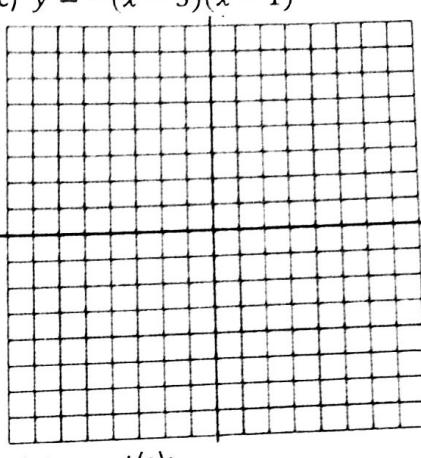
Decreasing:

Positive:

Negative:

End behavior:

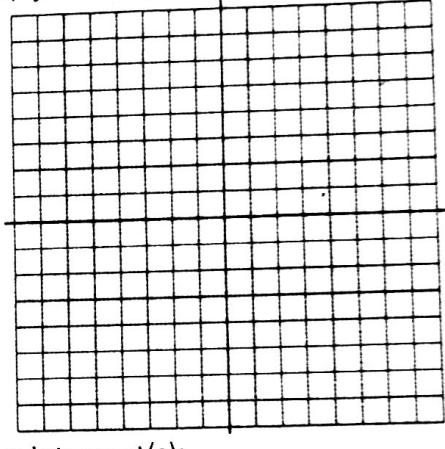
c) $y = -(x - 3)(x - 1)$



x-intercept(s):

Vertex:

f) $y = -2(x + 4)(x + 2)$



x-intercept(s):

y-intercept:

Axis of Symmetry:

Vertex:

Max/min value:

Domain:

Range:

Increasing:

Decreasing:

Positive:

Negative:

End behavior: