

5.4 Piecewise Functions

Evaluate the following functions.

$$1) f(x) = \begin{cases} (x+1)^2, & x < 2 \\ x^2 + 3, & x \geq 2 \end{cases}$$

a)  $f(-3)$

b)  $f(7)$

c)  $f(2)$

$$3) h(x) = \begin{cases} 3x + 2, & x \leq -1 \\ x - 2, & -1 < x \leq 4 \\ 2x - 5, & x > 4 \end{cases}$$

a)  $h(-4)$

b)  $h(-1)$

c)  $h(4)$

d)  $h(10)$

$$2) g(x) = \begin{cases} -x^2 + 1, & x < -4 \\ 2|x| - 4, & -4 \leq x < 5 \\ x - 7, & x \geq 5 \end{cases}$$

a)  $g(3)$

b)  $g(-12)$

c)  $g(5)$

$$4) k(x) = \begin{cases} 3x^2 + 2, & -9 \leq x < -1 \\ x - 5, & -1 < x \leq 4 \\ |x|, & x > 4 \end{cases}$$

a)  $k(-4)$

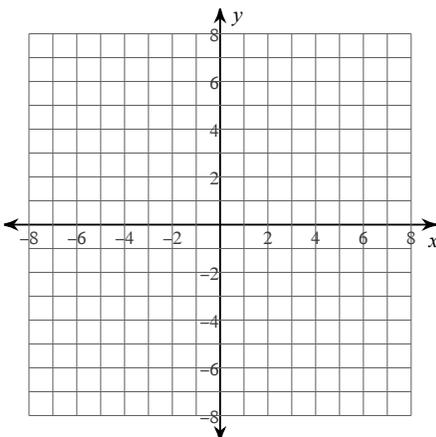
b)  $k(-1)$

c)  $k(4)$

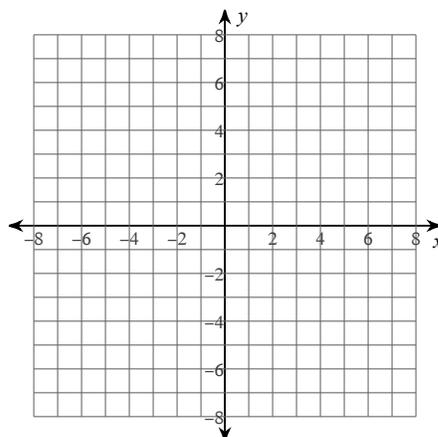
d)  $k(7)$

Sketch the graph of each function.

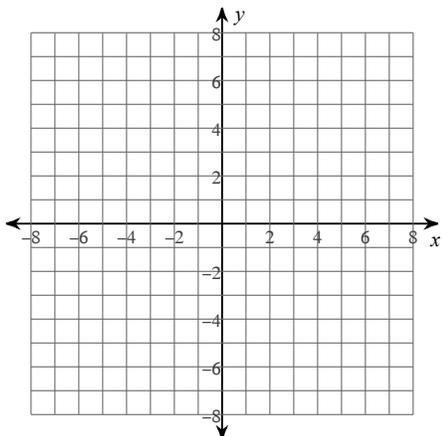
$$5) f(x) = \begin{cases} -2, & x \leq -4 \\ (x+4)^2, & x > -4 \end{cases}$$



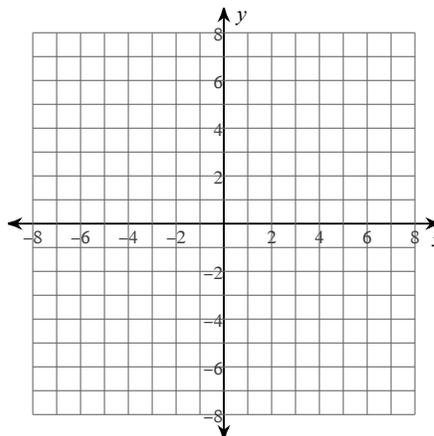
$$6) f(x) = \begin{cases} -x - 2, & x \leq -3 \\ 4 - x^2, & -3 < x \leq 3 \\ -x + 2, & x > 3 \end{cases}$$



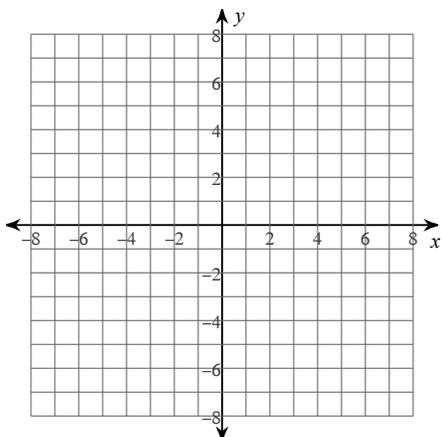
$$7) f(x) = \begin{cases} x + 1, & x < 0 \\ -x + 3, & x = 0 \\ (x - 3)^2, & x > 2 \end{cases}$$



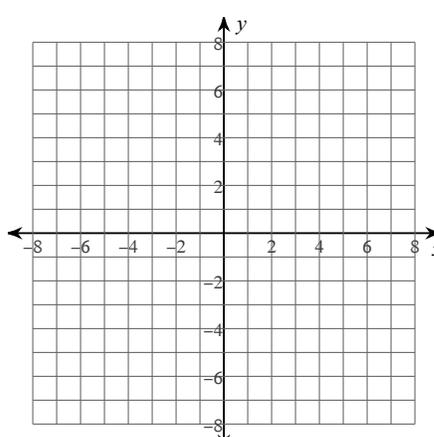
$$8) f(x) = \begin{cases} 0, & x \leq 0 \\ (x - 2)^2, & 0 < x \leq 4 \\ x - 1, & x > 4 \end{cases}$$



$$9) g(x) = \begin{cases} 3, & x \leq 0 \\ 2x + 3, & x = 1 \\ |x - 4|, & x > 1 \end{cases}$$

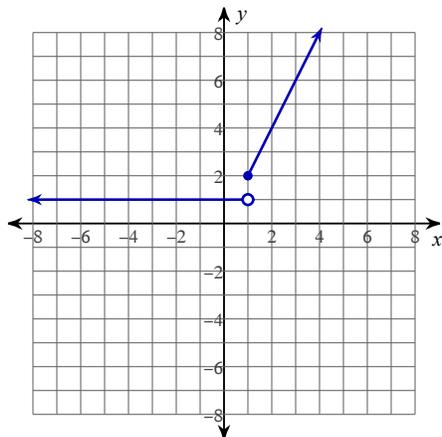


$$10) h(x) = \begin{cases} (x + 2)^2, & x < -1 \\ |x - 3|, & -1 \leq x < 4 \\ -|x|, & x \geq 4 \end{cases}$$

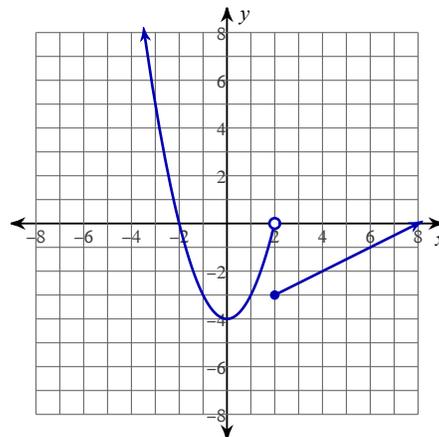


Write an equation for each piecewise function.

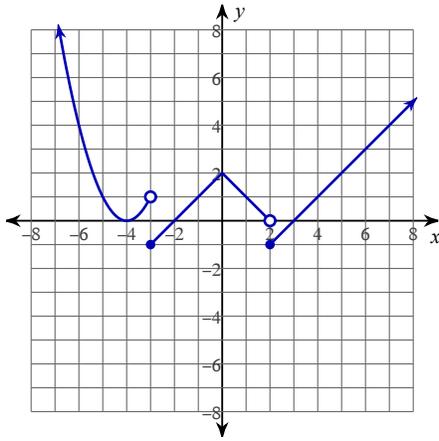
11)



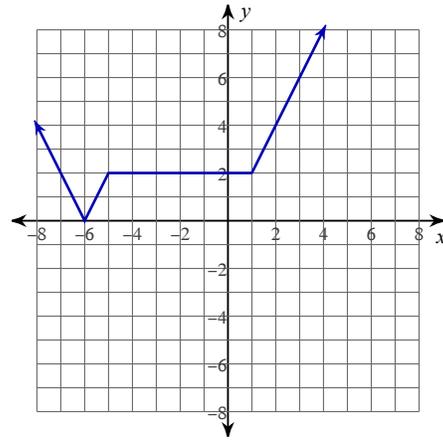
12)



13)



14)



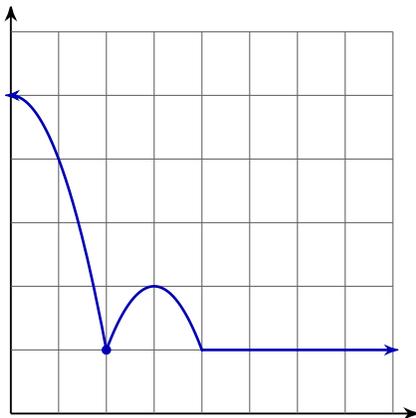
**Sketch a graph that could model each situation.**

15) Steven is driving to the store. He stops at a light half way there. He arrives and finds the store is closed so he goes home.

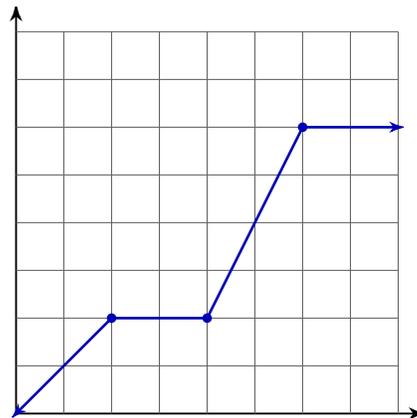
16) Every time Samantha trains for a 5k race she starts with a 5 min sprint, then jogs for 20 min, and then walks for 5 min.

**Write a situation that could be modeled by the graph.**

17)



18)



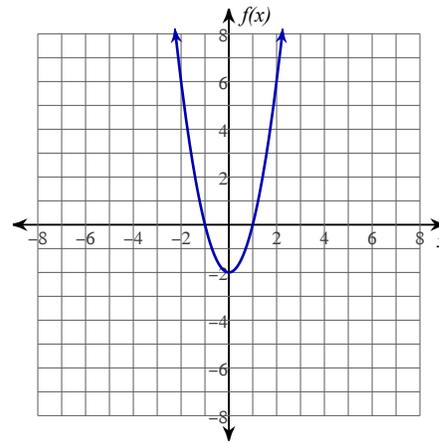
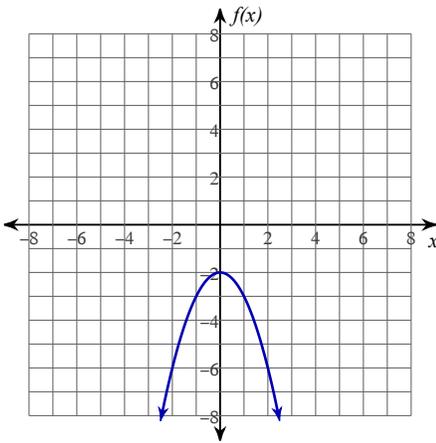
For each problem, find the average rate of change of the function over the given interval.

19)  $f(x) = x^2 + 1$ ;  $[-2, 0]$

20)  $f(x) = -x^2 + 2$ ;  $[-3, -\frac{5}{2}]$

21)  $f(x) = -x^2 - 2$ ;  $[-2, 1]$

22)  $f(x) = 2x^2 - 2$ ;  $[0, 1]$



23)  $f(x) = -2x^2 + 1$ ;  $[-2, 0]$

24)  $f(x) = x^2 + 2x - 2$ ;  $[-3, -1]$

