3.1 Greatest Common Factor

Simplify.
$$2(5x^2 - 3x + 7)$$

b.
$$\widehat{x(x-4)}$$

c.
$$3x^2(x-2x+8)$$

$$-3x^3 + 24x^2$$

2) Find the term that makes the two expressions equivalent.

d.
$$x^2 + 3x - 40 = (x + 8)(x - 5)$$

$$x^2 - 5x + 8x - 40$$

e.
$$x^2 - \frac{7x}{4} - 30 = (x - 10)(x + 3)$$

$$x^2 + 3x - 10x - 3$$

 $x^2 - 5x + 8x - 40$ $x^2 + 3x - 10x - 30$ We are used to starting with two multiples and distributing, but sometimes we want to work backwards from an expression to see the multiples at the first starting of the see the multiples at the first starting of the see the multiples at the first starting of the see the multiples at the first starting of the see the multiples at the first starting of the see the multiples at the first starting of the see the multiples at the first starting of the see the multiples at the first starting of the see the multiples at the first starting of the see the multiples at the first starting of the see the multiples at the first starting of the see the multiples at the first starting of the see the second of the sec an expression to see the multiples that it came from.

Factoring: Norking backwards from distribution to see what multiples an expression came from

The reason we care so much about factoring is because it helps us find solutions to equations. We will talk about that more in unit 4.

There are lots of different strategies to factor, but the first method you should always check for is the greatest

Greatest Common Factor: The biggest multiple each term has in common

Types of GCFS

- 1) Coefficients 2) Negatives 3) Variables
- 4) Any combo of the

To check if there is a coefficient as a GCF, look for the biggest number that every coefficient is divisible by.

3) Factor the greatest common factor out of each expression.

a.
$$10x^2 - 6x + 14$$

$$2(5x^2-3x+7)$$

ession.
b.
$$15x^3 - 5x^2 - 20x + 5$$

$$5(3x^3-x^2-4x+1)$$

c.
$$27x + 30$$

 $3(9x + 10)$

d.
$$6x^2 + 18x - 24$$

 $6(x^2 + 3x - 4)$

Negatives

If the first term of an expression is negative, then we will factor out the negative. Because of this, it is super important that your expression is in Standard form before you start factoring.

4) Factor the greatest common factor out of each expression.

a.
$$-x^2 - 4x + 6$$

- $(x^2 + 4x - 6)$

c.
$$8m^3 - 2m^8 + 7m^6$$

 $-2m^8 + 7m^6 + 8m^3$
 $-(2m^8 - 7m^6 - 8m^3)$

*When you factor when you factor when you factor when
$$3b^2 - 2b^4 - 7b$$
 and a negative, switch all the signs $-(2b^4 - 3b^2 + 7b)$

d.
$$-5y^6 + y^3 - y$$

- $(5y^6 - y^3 + y)$

Variables

If every term has the same variable (even if the exponents are different), then you will have a variable as a GCF. Whatever the smallest exponent is is the amount of the variable that you can factor out from each term.

5) Factor the greatest common factor out of each expression b. $6x^5 + 2x^4 - x^3$

a.
$$8m^8 - m^6$$

$$m^6 (8 m^2 - 1)$$

$$x^{3}(6x^{2} + 2x - 1)$$

$$d = -7y^{4} + 21y^{7} + 2y^{5}$$

c.
$$-3x^3 + 7x^4 + 24x^2$$

 $7x^4 - 3x^3 + 24x^2$
 $x^2 (7x^2 - 3x + 24)$

d.
$$-7y^4 + 21y^7 + 2y^5$$

 $21y^7 + 2y^5 - 7y^4$
 $y^4(21y^3 + 2y - 7)$
rt putting them all together:
Look for any combe
ession.
b. $-x^5 + 7x^4 - 2x$ of the three
 $-x(x^4 + 7x^3 - 2)$ other strategies

Now that we've seen each of these individually, let's start putting them all together:

6) Factor the greatest common factor out of each expression.

a.
$$8a^8 - 4a^4 + 16a^2$$

 $4a^2 (2a^6 - a^2 + 4)$

c.
$$25c^4 + 15c^6 + 40c^5$$

 $15c^6 + 40c^5 + 25c^4$
 $5c^4 (3c^2 + 8c + 5)$
e. $36c^5 + 60c^7 - 12c^9$
 $-12c^9 + 60c^7 + 36c^5$

$$-12c^{9} + 60c^{7} + 36c^{5}$$

$$-12c^{5}(c^{4} - 5c^{2} - 3)$$

b.
$$-x^5 + 7x^4 - 2x$$

 $-x(x^4 + 7x^3 - 2)$

d.
$$3m^3 - 12m^6$$

 $-12m^6 + 3(m^3)$
 $-3m^3(4m^3 - 1)$

Factoring by Grouping

If you are given four terms and are asked to factor, you may want to consider factoring by grouping. When we ctor by grouping, we are going to split the expression into groups and take the GCF out of each group.

What is the first thing you always look for when you factor? <u>CCF</u>

Steps to factoring by grouping:

i) Split in half

- 2) Factor out GCF from each half
- 3) GCFs make their own parentheses followed by repeated pasentheses

a) $4x^2 + 20x + 3xy - 15y$ * Notice how 2) 4x(x+5) - 3y(x+5) repeated repeated poventhese 3) (4x-3y)(x+5)

b) $3x^3 - 6x^2 + 15x - 30$

(a) $4x^3 + 8x^2 + x + 2$ (b) $4x^2 + 1 + 1 + 2$ (c) $4x^3 + 8x^2 + x + 2$ (d) $4x^2 + 1 + 1 + 2$ (d) $4x^2 + 1 + 2$

e) $x^2y - 3x^2 - 8y + 24$

*If there is no GCF, factor d) 3xy - 21y 5x - 353y(x-7)+5(x-7) (3y+5)(x-7)

f) $8x^3 + 6x^2 - 24x - 18$