4.1: Simplifying Rational Expressions

1) The length of a rectangular prism is 9 more than the width. The volume is $x^3 + 8x^2 - 9x$. What is the simplified expression for the height of the prism?

- 2) Write a rational expression that has 4 and -3 as excluded values.
- 3) A square has a side length of x + 4 and a rectangle with height 2x+8 has the same area as the square. What is the length of the rectangle?

Simplify each and state the excluded values.

4)
$$\frac{k+3}{k^2+8k+15}$$

$$5) \ \frac{x^2 + 2x + 1}{x + 1}$$

6)
$$\frac{n-2}{n^2 - 7n + 10}$$

7)
$$\frac{20n^2 + 12n}{12n}$$

8)
$$\frac{6b^2 - 14b}{4b^2 + 6b}$$

9)
$$\frac{b^2+b-12}{b^2-9b+18}$$

10)
$$\frac{9m-27}{m^2-11m+24}$$

11)
$$\frac{n^2 + 6n + 9}{n^2 + 9n + 18}$$

$$12) \ \frac{21p^2 + 35p}{21p^2 - 28p}$$

13)
$$\frac{r^2 - 6r + 9}{r^2 - 10r + 21}$$

14)
$$\frac{n^2 - 36}{n^2 - n - 42}$$

15)
$$\frac{k^2 + 14k + 48}{k^2 - 4k - 60}$$

$$16) \ \frac{18x^3 + 30x^2 + 12x}{42x^3 + 90x^2 + 12x}$$

$$17) \ \frac{2x+16}{5x^3+39x^2-8x}$$

Perform the following operations

18)
$$\frac{1}{3} \cdot \frac{2}{5}$$

19)
$$\frac{11}{5} \div 2$$

20)
$$\frac{3}{4} + \frac{2}{3}$$

21)
$$\frac{8}{12} - \frac{3}{8}$$

SPIRAL REVIEW

22) Describe the end behavior both formally and informaly for the following polynomials and then state the possible number of turning points:

a)
$$f(x) = -x^4 + 4x^2 - 2$$

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$$f(x) = -x^7 + 9x^3 - x + 1$$

- 23) Graph the function $f(x) = -x^4 x^2 + 2$ and state the following:
 - a) Zeros:
 - b) Relative Minimums:
 - c) Relative Maximums:
 - d) y intercept:
 - e) Domain:
 - f) Range:

