

1.2 Polynomial Operations

Adding and subtracting polynomials

Anytime we need to add or subtract a polynomial, the big idea is to combine like terms

* Remember to write answers in standard form

1) Simplify each expression.

a. $(8p^2 - 7p) - (p - p^2)$

$$\begin{array}{r} 8p^2 - 7p - p + p^2 \\ \hline 9p^2 - 8p \end{array}$$

c. $(2n - 7) + (2n + 3)$

$$\begin{array}{r} 2n - 7 + 2n + 3 \\ \hline 4n - 4 \end{array}$$

e. $(6 - 3x^3 - 8x^4) + (5 + 7x^4)$

$$\begin{array}{r} 6 - 3x^3 - 8x^4 + 5 + 7x^4 \\ \hline -x^4 - 3x^3 + 11 \end{array}$$

b. $(5 - 3m^2) - (6 - 8m^2)$

$$\begin{array}{r} 5 - 3m^2 - 6 + 8m^2 \\ \hline 5m^2 - 1 \end{array}$$

If you're adding, you can drop the parentheses & combine like terms

d. $(k^3 - 3) + (5 + 6k^3)$

$$\begin{array}{r} k^3 - 3 + 5 + 6k^3 \\ \hline 7k^3 + 2 \end{array}$$

f. $(7p - 7p^4 + 3p^2) - (6p^3 + 1)$

$$\begin{array}{r} 7p - 7p^4 + 3p^2 - 6p^3 - 1 \\ \hline -7p^4 - 6p^3 + 3p^2 + 7p - 1 \end{array}$$

Subtraction is like distributing a negative

Multiplying polynomials

Multiplying polynomials is another use of the distributive property. This time we will make sure that we distribute each term in the first polynomial to each term in the second polynomial.

Distribute: multiply to each term

2) Simplify each expression.

a. $(3x + 6)(2x + 6)$

$$6x^2 + 18x + 12x + 36$$

$$\boxed{6x^2 + 30x + 36}$$

c. $(3n - 4)(8n - 2)$

$$24n^2 - 6n + 32n + 8$$

$$\boxed{24n^2 + 26n + 8}$$

e. $(3m - 2)(7m^2 - 5m + 2)$

$$\begin{array}{r} 21m^3 - 15m^2 + 6m \\ - 14m^2 + 10m - 4 \\ \hline 21m^3 - 29m^2 + 16m - 4 \end{array}$$

g. $(7x^3 - 4x^2 + 1)(4x + 2)$

$$\begin{array}{r} 28x^4 + 14x^3 \\ - 16x^3 - 8x^2 \\ \hline + 4x + 2 \end{array}$$

$$\boxed{28x^4 - 2x^3 - 8x^2 + 4x + 2}$$

b. $(2v - 4)(3v - 1)$

$$6v^2 - 2v - 12v + 1$$

$$\boxed{6v^2 - 14v + 1}$$

d. $(5b + 1)(7b - 6)$

$$35b^2 - 30b + 7b - 6$$

$$\boxed{35b^2 - 23b - 6}$$

f. $(8n - 6)(5n^2 - n - 1)$

$$\begin{array}{r} 40n^3 - 8n^2 - 8n \\ - 30n^2 + 6n + 6 \\ \hline 40n^3 - 38n^2 - 2n + 6 \end{array}$$

h. $(3x + 4)^2$

$$(3x+4)(3x+4)$$

Something squared means it is multiplied by itself, so we have to write it out twice.

$$9x^2 + 12x + 12x + 16$$

$$\boxed{9x^2 + 24x + 16}$$